

$$x + jy = r \cos(\theta) + j r \sin(\theta)$$

$$= r [\cos(\theta) + j \sin(\theta)] = r \angle \theta$$

where $r = \sqrt{x^2 + y^2}$, $\theta = \tan^{-1}\left(\frac{y}{x}\right)$

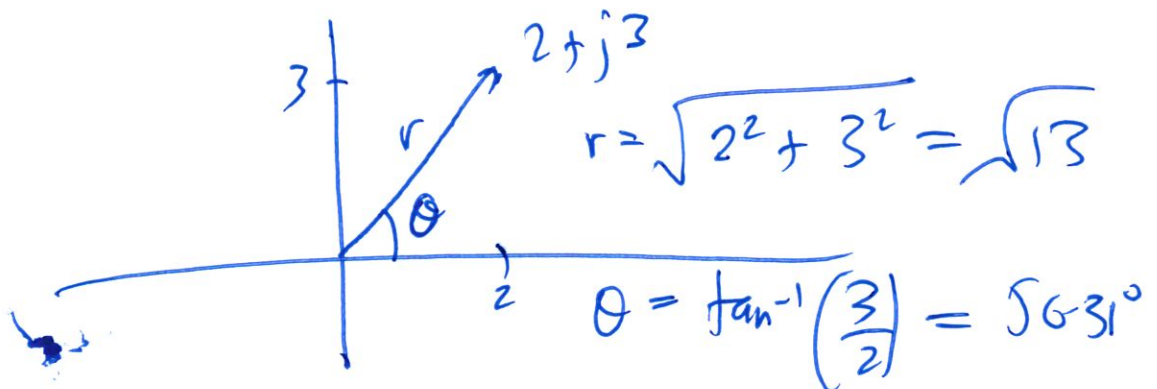
r is called the modulus of $z = x + jy$

θ is called the argument of $z = x + jy$.

$-180^\circ \leq \theta \leq +180^\circ$ — principal argument.

Express $2 + j3$ in polar form.

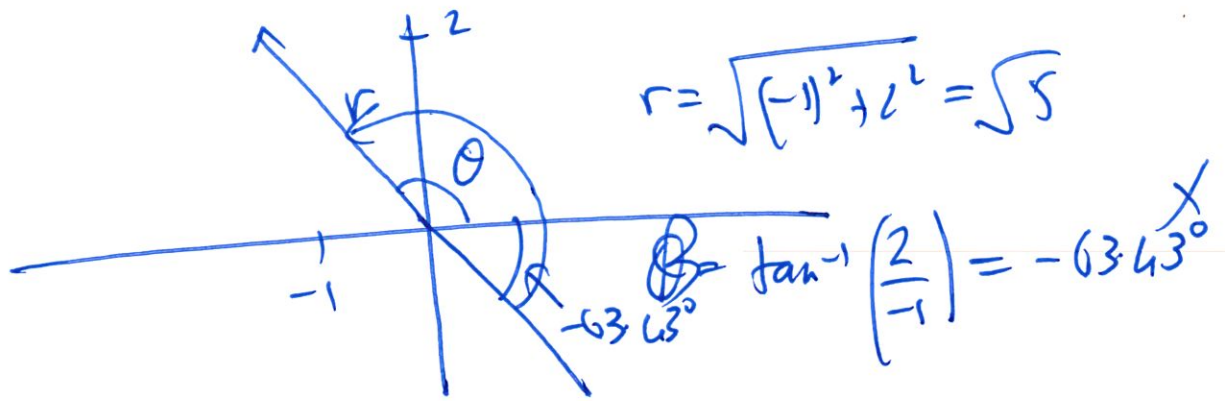
Soln,



$$2 + j3 = \sqrt{13} \angle 56.31^\circ$$

$-1 + j2$ into polar form.

Soln:



$$r = \sqrt{(-1)^2 + 2^2} = \sqrt{5}$$

$$\tan^{-1}\left(\frac{2}{-1}\right) = -63.43^\circ$$

$$\theta = 180^\circ - 63.43^\circ$$

$$= 116.57^\circ$$

$$-1 + j2 = \sqrt{5} \angle 116.57^\circ$$

$$2 = 2 + j0 = 2 \angle 0^\circ$$



$$j2 = 2 \angle 90^\circ$$



$$-2 = 2 \angle 180^\circ$$

$$-j2 = 2 \angle 270^\circ \text{ or } 2 \angle -90^\circ$$

Express $2 \angle 53^\circ$ into $x + jy$ form.

$$r \angle \theta = r \cos(\theta) + j r \sin(\theta)$$

$$2 \angle$$

$$\begin{aligned} 2 \angle 53^\circ &= 2 \cos(53^\circ) + j 2 \sin(53^\circ) \\ &= 1.2 + j 1.6 \end{aligned}$$

11.1

$$\frac{3-j4}{2} = \frac{3}{2} - j\frac{4}{2} = 1.5 - j2$$

$$\frac{5-j3}{3+j4} = \frac{(5-j3)(3-j4)}{(3+j4)(3-j4)}$$

$$= \frac{15 - j20 - j9 + j^2 12}{3^2 + 4^2}$$

$$= \frac{15 - j29 - 12}{25}$$

$$= \frac{3 - j29}{25} = \frac{3}{25} - j\frac{29}{25}$$

Let $Z = 100 - j25$. Find $\frac{1}{Z}$

Soln: $\frac{1}{Z} = \frac{1}{100 - j25}$

$$= \frac{1}{25} \cdot \left(\frac{4-j}{4-j} \right)$$

$$= \frac{1}{25} \left(\frac{4+j}{17} \right) = \frac{1}{25 \times 17} (4+j)$$